

# r2ogs6: An R wrapper of the OpenGeoSys 6 Multiphysics Simulator

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#### **Software**

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- [Repository](https://github.com/joboog/r2ogs6) C
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### **Summary**

Understanding the impacts of climate change and hydrologic extreme events on our sub–surface earth system is even in temperate zones of utmost importance [\(Felfelani et al., 2017;](#page-6-0) [Field](#page-6-1) [et al., 2012;](#page-6-1) [Wu et al., 2020\)](#page-8-1). Key tools to develop such understanding are physics–based simulation models that describe the manifold interactions of involved natural phenomena across time and space [\(X. Li et al., 2023;](#page-7-0) [Steefel et al., 2015\)](#page-7-1).

Our package r2ogs6 provides a file–based interface of the multi–physics simulation code OpenGeoSys 6 [\(Bilke et al., 2019;](#page-6-2) [Kolditz et al., 2012\)](#page-7-2) to the [R](www.r-project.org) programing and statistical computing environment. r2ogs6 enables R users to perform and analyze simulation models of the sub–surface earth system in R. It allows to access the capabilities of OpenGeoSys 6 to simulate thermo-hydro-mechanical-chemical and biological (THMC/B) processes in porous and fractured media within R. In this way, r2ogs6 enables R users to model sub–surface phenomena and technologies such as groundwater flow, reactive transport, geothermal energy usage and/or nuclear waste repositories as well as to analyze and further process simulation output. r2ogs6 enables users to prepare and manipulate OpenGeoSys 6 simulation models, run the simulations and retrieve corresponding output, all within an R session or simple R scripts. Therefore, R classes and functions were designed to communicate with the respective OpenGeoSys 6 input and output files as well as executables. In addition to single-simulation runs, r2ogs6 supports ensemble runs that can be used to set up uncertainty and sensitivity analyses as well as parameter studies. Furthermore, r2ogs6 allows conducting and documenting OpenGeoSys 6 simulations in reproducible R scripts or notebooks. As OpenGeoSys 6 is continuously being developed further, code generation functions for r2ogs6 developers were included to speed up the package updating process in case of future changes to OpenGeoSys 6.

r2ogs6 was designed to be used by domain researchers, data scientists and students working with OpenGeoSys 6. Moreover, r2ogs6 was intended to include OpenGeoSys 6 into R based scientific workflows and aims to bridge the gap between data produced by a scientific simulation code and data science.

## **Statement of need**

Major challenges humanity has to face in the coming decades are climate change and hydrologic extremes [\(Field et al., 2012\)](#page-6-1). Understanding the impacts of climate change and hydrologic

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extreme events on our sub–surface earth system is even in temperate zones of utmost importance for ensuring adequate domestic and drinking water supplies, together with functioning lake and river systems with healthy aquatic ecosystems and ecosystem services [\(Felfelani et al.,](#page-6-0) [2017](#page-6-0); [Wu et al., 2020\)](#page-8-1). Of course, the needs of the population and the needs of nature are often in conflict, which increases the necessity to study the complex interaction of both within different scenarios. The core of such studies is most often the system and scenario analysis of individual or coupled earth systems compartments through physics simulations [\(X. Li et al.,](#page-7-0) [2023;](#page-7-0) [Steefel et al., 2015\)](#page-7-1). In physics simulation models, multiple coupled natural processes are implemented, which are usually described with partial differential equations. Solving these equations requires appropriate numerical methods such as the finite element method (FEM). For reasons of performance, (multi) physics simulators are mostly implemented in languages such as FORTRAN, C or C++ [\(Steefel et al., 2015\)](#page-7-1).

One of these simulators is OpenGeoSys (OGS) (https://www.opengeosys.org/), a scientific open source project for the development of numerical methods to simulate thermo-hydromechanical-chemical and biological (THMC/B) processes in porous and fractured media [\(Bilke](#page-6-2) [et al., 2019](#page-6-2); [Kolditz et al., 2012\)](#page-7-2). OGS has applications ranging from small-scale geotechnical investigations [\(Grunwald et al., 2020\)](#page-7-3), to reservoir studies [\(D. Li et al., 2014\)](#page-7-4), nuclear waste repositories [\(Pitz et al., 2023\)](#page-7-5) and even groundwater management of entire landscapes [\(Jing](#page-7-6) [et al., 2018](#page-7-6); [Pujades et al., 2023\)](#page-7-7).

To identify the right action needs and to derive further decision support for the above described problems it often requires to explore several problem scenarios through meaningful model ensembles. This translates to more and more complex and larger model setups [\(Asher et al.,](#page-6-3) [2015](#page-6-3)). Thus, faster and more efficient model setup and parametrization procedures are needed. But while OpenGeoSys is a powerful FEM code, setting up, running and evaluating multiple simulations can prove complicated.

Here is where languages such as R and Python can prove useful. Via an interface that adds a layer on top of OpenGeoSys 6, the user can access preprocessing tools, the solver itself and postprocessing tools alike, thus increasing usability and accessibility. The development and application of high–level programming and/or scripting languages interfaces to geoscientific simulators has been gaining increasing attention in recent years. Examples are FloPy: a Python interface to the groundwater simulator Modflow Langevin et al. [\(2021\)](#page-7-8), RedModRPhree: an R package with utility functions to the geo-chemical solver Phreeqc Charlton & Parkhurst [\(2011\)](#page-6-4), the toughio Python interface to the multi-phase flow simulator TOUGH Pruess [\(2004\)](#page-7-9), the Python interfaces to OpenGeoSys 5: ogs5py [\(Müller et al., 2021\)](#page-7-10) and OpenGeoSys 6: ogs6py [\(Buchwald et al., 2021\)](#page-6-5) as well as the R interface to OpenGeoSys 5: r2ogs5 [\(Schad et](#page-7-11) [al., 2023](#page-7-11)). FloPy, ogs5py, ogs6py and r2ogs5 provide object-oriented frameworks to set-up, call the executables and import the output of the associated simulators. The idea of these packages is to provide Python and R functions to pre- and process simulation data but to just run simulations via a call to the the operating system to execute the simulators with the prepared input. RedModRPhree and toughio rather focus on additional pre- and post processing functions to simplify the set-up of simulations with R and Python. These packages still rely on external execution of the associated simulation program.

Altough there already exist the OpenGeoSys 6 Python interface ogs6py, we consider an R interface to be just as important, as R is a well known language in the environmental and geosciences. Furthermore, since R is a popular language in the field of data science with many powerful packages for data analysis and vizualisation, e. g. dplyr [\(Wickham, François, et al.,](#page-8-2) [2021\)](#page-8-2) and ggplot2 [\(Wickham, Chang, et al., 2021\)](#page-8-3), it's a natural choice for processing data generated by simulation tools such as OpenGeoSys 6. r2ogs6 follows a similar design approach compared to FloPy, ogs5py, ogs6py and r2ogs5: it provides an object-oriented approach with R classes and functions to set-up an OpenGeoSys 6 simulation, call the respective executable and import the output of finished simulations (see section Package Structure for more details).

Moreover, r2ogs6 can facilitate the calibration of OpenGeoSys 6 models. One possibility is to use implemented functions to design ensemble runs. A second possibility is to use available R



packages for model calibration such as lhs [\(Carnell, 2021\)](#page-6-6), mlrBO [\(Bischl et al., 2017\)](#page-6-7). For R users who do not have a lot of (or any) experience with environmental and geoscientific sub–surface simulations, yet an interest in such, r2ogs6 provides a good starting point. Utilizing r2ogs6, users can easily set up their first OpenGeoSys 6 simulations by choosing one of the provided benchmark files. Moreover, with R scripts and R--Markdown or JupyteR notebooks, modeling workflows can easily be documented, published and shared with peers.

r2ogs6 has already been applied in [\(Heinrich, 2021\)](#page-7-12), where its ensemble functionality was tested utilizing the OpenGeoSys 6 Theis' problem benchmark files [\(Walther, 2020;](#page-8-4) [Wang,](#page-8-5) [2020\)](#page-8-5); or to calibrate groundwater flow models [\(Boog et al., 2021\)](#page-6-8).

# **Package Structure**

r2ogs6 is thought to set up an OpenGeoSys 6 simulation inside an R session by executing specified model creation functions or by reading existing OpenGeoSys 6 input files. With further functions, the simulation can be executed and corresponding output can be read into the R session again. [Figure 1](#page-3-0) highlights the structure of r2ogs6. The central element that represents an OpenGeoSys 6 simulation is the OGS6 object, which is an instance of a R6 class. This object represents a single simulation; multiple simulations can be defined with the OGS6\_Ensemble class. An OGS6 object contains several child objects that represent the simulation input and output. The main OpenGeoSys 6 input files are the project file  $\star$ .prj, geometry file  $\star$ .gml and input FEM mesh file(s)  $*$ . vtu. These are read in or written via S3 class based functions (block read\_in\* / export\* in [Figure 1\)](#page-3-0). When reading in, the  $XML$ –based \*.prj input file is parsed. Individual tags are represented as S3 class objects which are available via active fields in the 0GS6 object. Individual  $\star$ , prj tags may change due to ongoing development activities in OpenGeoSys 6, therefore, future updates of the related classes may be necessary. To simplify updates like this, helper functions for analyzing \*.prj files as well as suggesting and creating classes were implemented.

As the  $\star$ , gml and the  $\star$ , vtu files are less complex and less likely to change, these files are represented as R6 class objects and also available as active fields inside the OGS6 object. To execute simulations, functions for writing the OpenGeoSys 6 input (ogs6\_export\_simfiles()) and call the OpenGeoSys 6 executable (ogs6\_run\_simulation()) were implemented. Note that an OpenGeoSys 6 executable or singularity container needs to be present. Default executables and paths can be defined in a configuration file.

During execution OpenGeoSys 6 generates output data as \*.vtu files. These files are produced at user defined timesteps of the simulation and are referenced in a  $\star$ , pvd file. The function ogs6\_read\_output\_files() then attaches the output files to the OGS6 object as OGS6\_pvd objects (which in turn reference OGS6\_vtu objects). In this way, all data required for and produced by OpenGeoSys 6 can be represented as R native objects and results can be processed further using R functions.



<span id="page-3-0"></span>

**Figure 1:** Schematic of the r2ogs6 structure.

# **Examples**

### **Quick Start with Theis' Problem**

Theis' problem examines the lowering of the water level around a pumping well. Water is pumped from a well, which induces a lowering of the water level over time. The Theis' problem is a common benchmark for sub–surface flow simulators. See the respective desription on the OpenGeoSys 6 page [here.](https://www.opengeosys.org/docs/benchmarks/liquid-flow/liquid-flow-theis-problem/) The required input files are already present in the installed r2ogs6 package.

You can just create an .R script with the r2ogs6 commands to set-up a simulation from a benchmark file directly. Just load the package and get the path to the Theis' problem benchmark .prj file.

```
library(r2ogs6)
```

```
# Modify the prj_path depending on where you saved the benchmark file.
prj path <- system.file("extdata/benchmarks/AxiSymTheis/",
                        "axisym theis.prj", package = "r2ogs6")
```


Then define the path were the generated script is to be save (script path) and were the simulation is to be run (sim path). Note, that the folders should already exist. Finally, call the respective function to generate the script; the script will be named according to the name of the project file you specified but with the extension .R (here: axisym\_theis.R).

```
script path <- "path/to/scripts"
sim_path <- "path/to/sim"
ogs6_generate_benchmark_script(prj_path,
                               sim path = sim path,
                               script_path = script_path)
```
You can now open the generated script axisym\_theis.R and have a all the commands to generate and run a simulation object ready to explore.

### **Sensitivity Analysis of the Theis' Problem**

Here, we will set up an ensemble of models to visualize the sensitivity of the water level lowering to changes in the material specific parameter called storage.

The variable that corresponds to the water level is the pressure in the water, which increases with depth. So changes in storage will induce changes in the evolution of the pressure gradient around the well.

At first, load the required libraries.

```
library(r2ogs6)
library(ggplot2)
library(dplyr)
```
Then, create a simulation object to base the ensemble on and read in the .prj file.

```
# Change this to fit your system
testdir path \leq tempdir()
sim_path <- paste0(testdir_path, "/axisym_theis_sim")
```

```
# Create the simulation object
ogs6_obj <- OGS6$new(sim_name = "axisym_theis",
                     sim\_path = sim\_path)
```

```
# The input files should be present in your r2ogs6 installation directory
prj path <- system.file("extdata/benchmarks/AxiSymTheis/",
                        "axisym_theis.prj", package = "r2ogs6")
```

```
# Now read in the input files
read_in_prj(ogs6_obj, prj_path, read in qml = T)
```
To examine the effects of storage we change it by 1%, 10% and 50%. We can use the percentages mode parameter of OGS6 Ensemble for this.

```
# Assign percentages
percentages <- c(-50, -10, -1, 0, 1, 10, 50)
# Define an ensemble object
ogs6_ens <-
  OGS6_Ensemble$new(
    ogs6_obj = ogs6_obj,parameters = list(list(ogs6_obj$media[[1]]$properties[[4]]$value,
```


```
percentages)),
    percentages mode = TRUE)
Now start the simulation, read and visualize the output.
# Start the simulation
ogs6_ens$run_simulation()
# Attach the output files to the ensemble object.
lapply(ogs6_ens$ensemble, ogs6_read_output_files)
# Extract point specific data of the `pressure` variable from the output files
storage tbl \leqogs6\_ens$get\_point_data(point\_ids = c(0, 1, 2),keys = c("pressure")# Compute the spatial average of the pressure for all simulations
avg_pr_df <- storage_tbl %>%
  group_by(sim_id, timestep) %>%
  summarise(avg_pressure = mean(pressure))
# Plot the spatially averaged pressure over time for all simulations
ggplot(avg_pr_df, \text{aes}(x = as.numeric(as.factor(timestep)),y = avg pressure,
                      qroup = sim id)) +
  geom\_point(aes(color = as.factor(sim_id))) +geom line(aes(color = as.factor(sim id))) +
  \text{labs}(\text{color} = "sim id") +xlab("Timestep")
```
The plot then shows the development of the average pressure in each simulation of the ensemble over time.



**Figure 2:** plot of chunk p-t-all-combined-plot

Check the following package vignettes for more information: - a guide to set up a single simulation of a hydro-mechanics benchmark ( $\frac{\ln k}{n}$  - a guide to create ensemble runs ( $\frac{\ln k}{n}$  - a



development guide [\(link\)](https://joboog.github.io/r2ogs6/articles/dev_workflow_vignette.html)

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